



Из истории конференции

# Воспоминания участника

ELBRUS 2021, March 1-5



## Владимир Евгеньевич Фортов



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# Лев Владимирович Альтшулер



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# Давид Абрамович Киржниц



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## Москва Физматлит 2009 год



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# 2 конференции плывут по Енисею лето 1977 г.

**Александр Андреевич  
Самарский**

**Николай Николаевич  
Яненко**





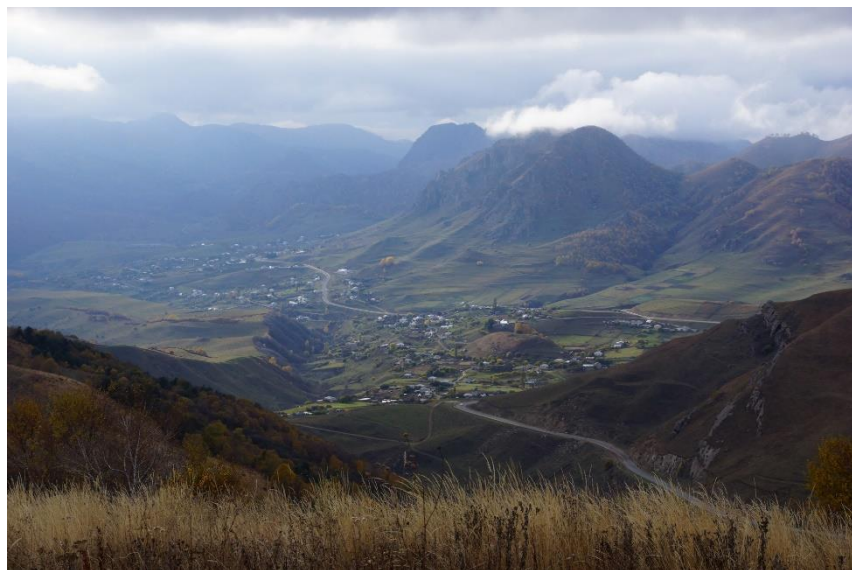
# Анатолий Индербиевич Темроков



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# Конец сентября – начало октября 1978 г. гост. Чегет 1-е рабочее совещание «УРС вещества»



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# Лето 1980 г. Голубые озера

## 2-е рабочее совещание «УРС вещества»



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# Весна 1982 г. гост. Иткол

## 3-е рабочее совещание «УРС вещества»



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# Начало января 1984 г. гост. Чегет 4-е рабочее совещание «УРС»



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# 1986 г. База КБГУ



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# 1988 г. и 1990 г. Пансионат «Вольфрам»



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# Эльбрус, март



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# Atomic number similarity law in individual electronic shells of all natural elements

*G.V. Shpatakovskaya*

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# Outline

- 1. Basis of the method used**
- 2. Algorithm of the method application**
- 3. Experimental data in atomic  $K$ ,  $L$ ,  $M$  shells**
- 4. Experimental and RLDA data in atomic  $N$ ,  $O$ ,  $P$  shells**
- 5. Reconstructed data**
- 6. Conclusion**





## 1.1 Basis of the method used

- The quantization condition:

$$S_{n0}(E) = \int \sqrt{2(E - U(r))} dr = \pi n, \text{ if } l = 0;$$

$$S_{nl}(E) = \int \sqrt{2(E - U(r) - \lambda^2/r^2)} dr = \pi(n - \lambda)$$

$$E_{nl}(Z) - E_{n0}(Z) \sim \lambda^2, \quad \lambda = l + 1/2$$

- Then electron energy levels **in TF atom** are

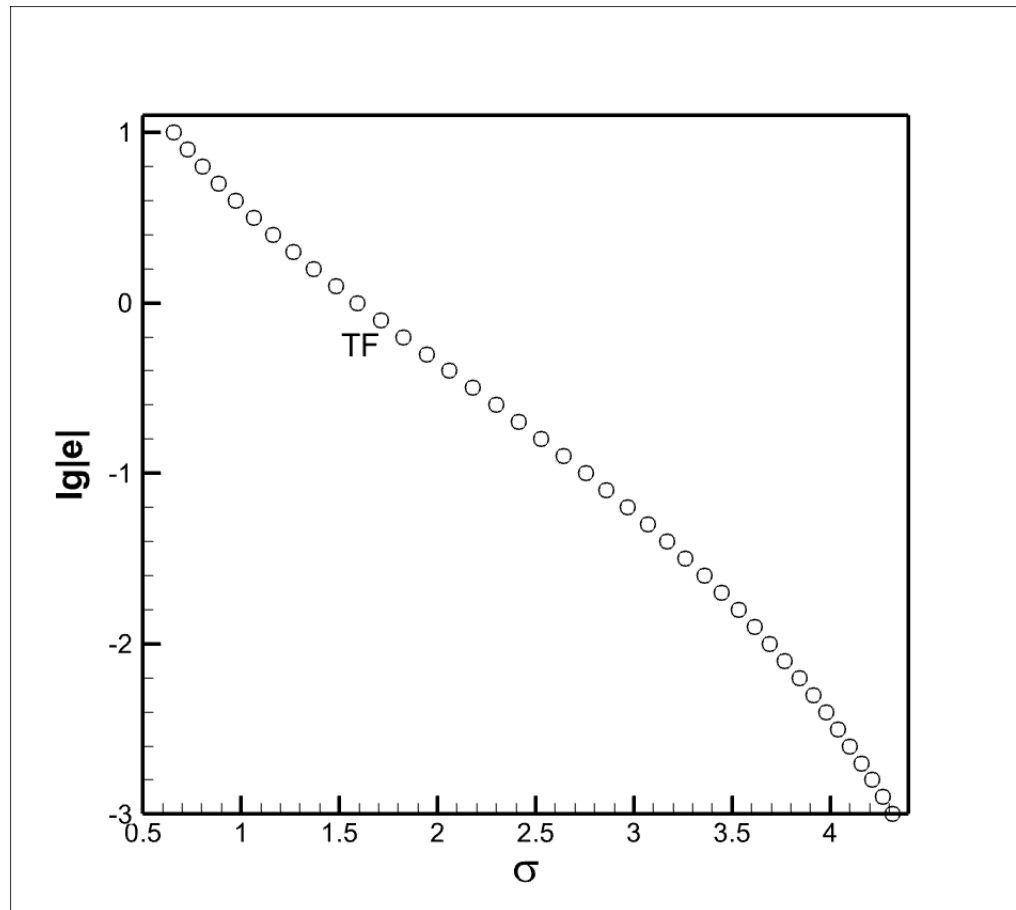
$$E_{n0}(Z) = Z^{4/3} e(\sigma_n), \quad \sigma_n = \pi n Z^{-1/3}, \text{ if } l = 0;$$

$$E_{nl}(Z) = E_{n0}(Z) + Z^{2/3} d(\sigma_n) \lambda^2$$

Where  $e(\sigma)$  and  $d(\sigma)$  are **universal** functions



## 1.2 Functions $e(\sigma)$ in TF model for atoms $Z = 10 - 92$





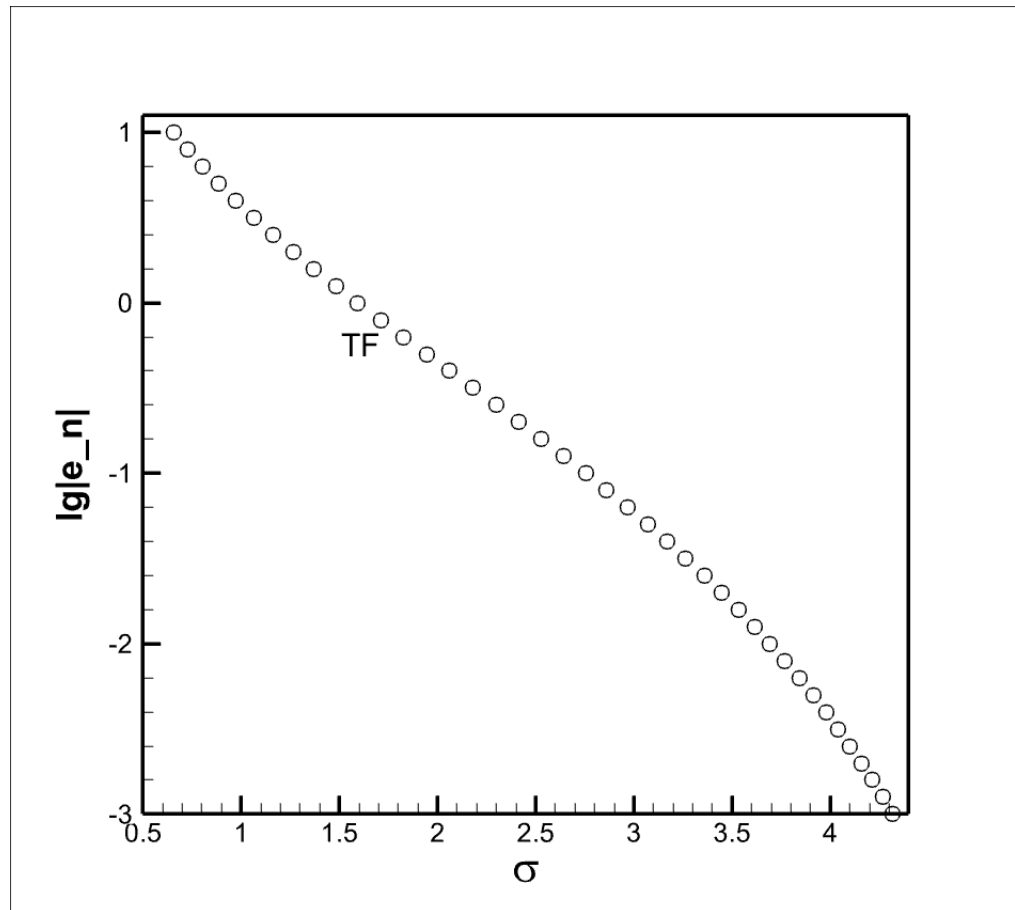
## 2.1 Algorithm for representing experimental electron binding energies (**EBE**) in atoms

$$e_n(\sigma_n) = \frac{E_{no}}{Z^{4/3}}, \quad \sigma = \frac{\pi n}{Z^{1/3}},$$

$$d_{nlj}(\sigma_n) = \frac{E_{nlj} - E_{no}}{(l + 1/2)^2 Z^{2/3}}, \quad j = l \mp 1/2$$

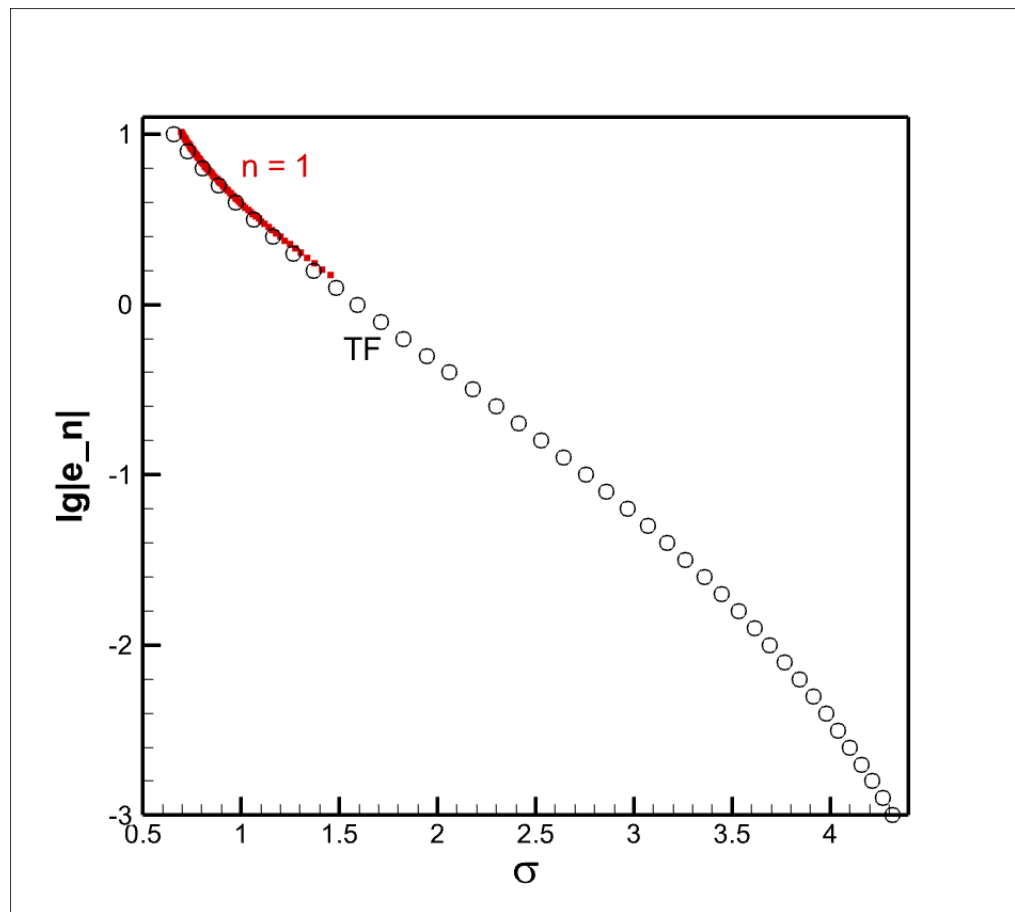


## 2.2 Functions $e(\sigma)$ , TF and reconstructed from all the experimental s-levels $E_{n0}$ for atoms $Z = 10 - 92$



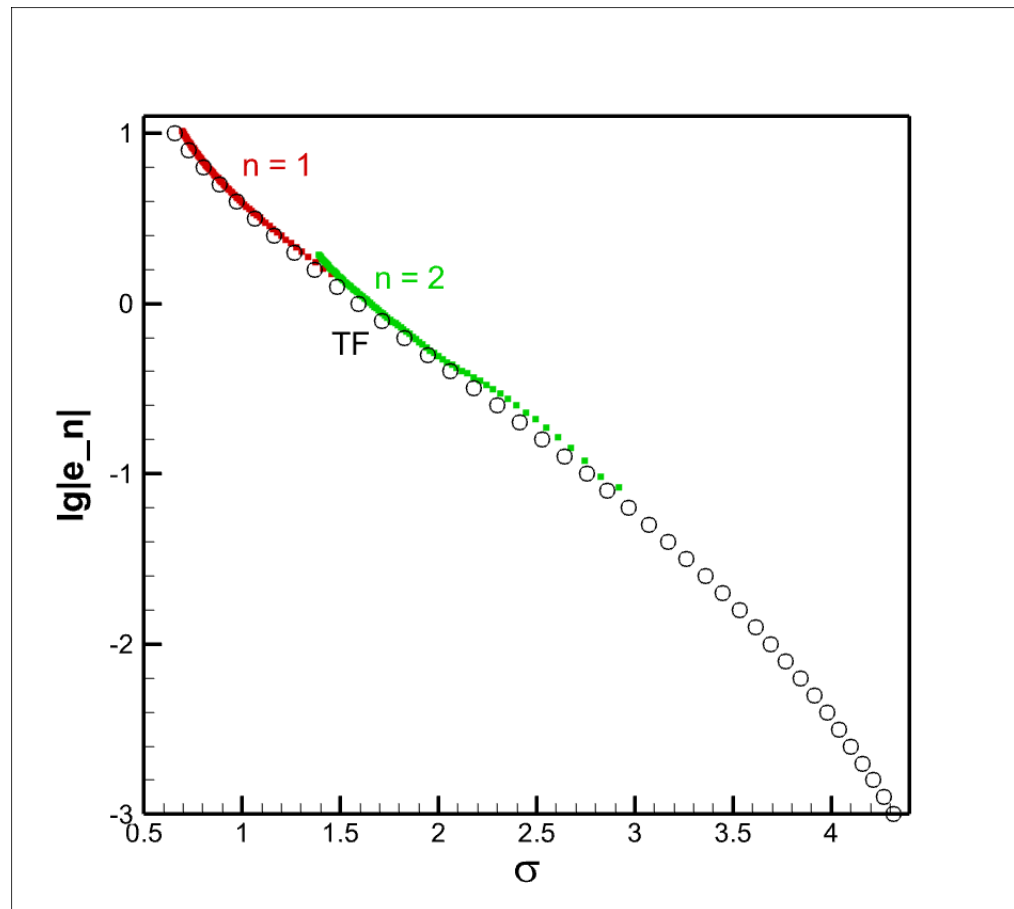


## 2.3 Functions $e(\sigma)$ , TF and reconstructed from all the experimental s-levels $E_{n0}$ for atoms $Z = 10 - 92$



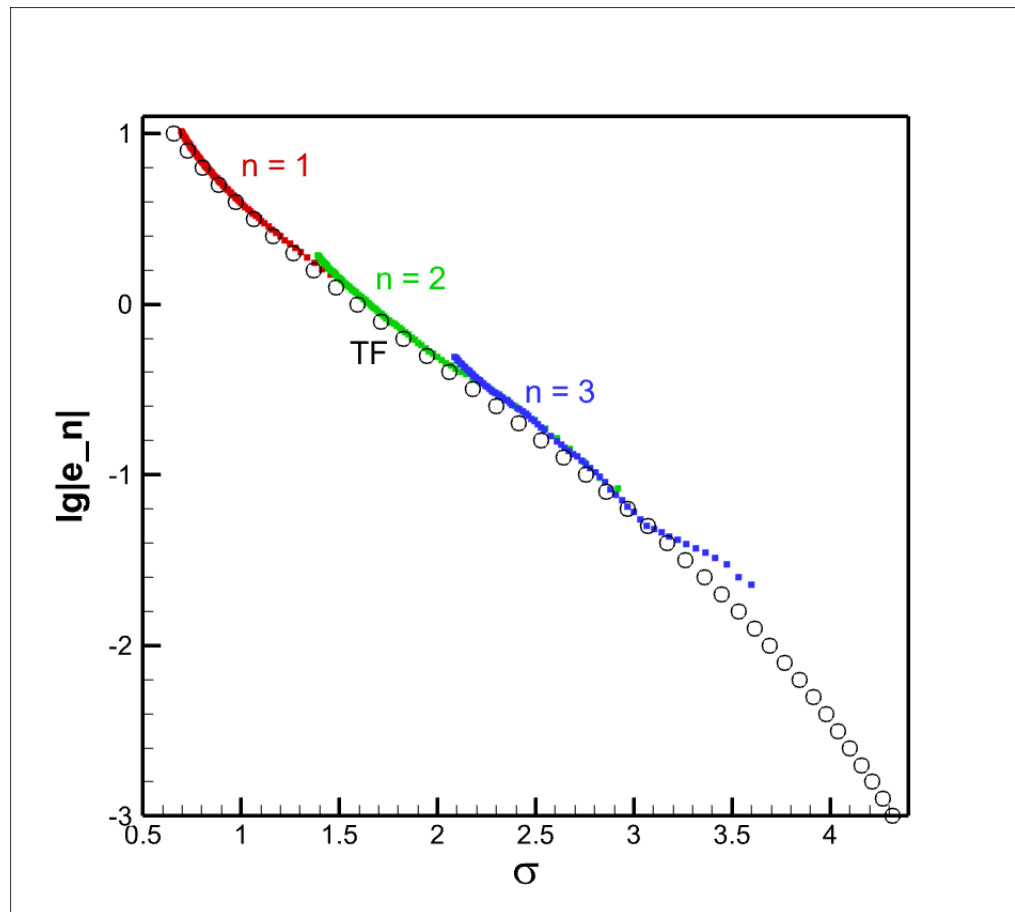


## 2.4 Functions $e(\sigma)$ , TF and reconstructed from all the experimental electron s-levels $E_{n0}$ for atoms $Z = 10 - 92$



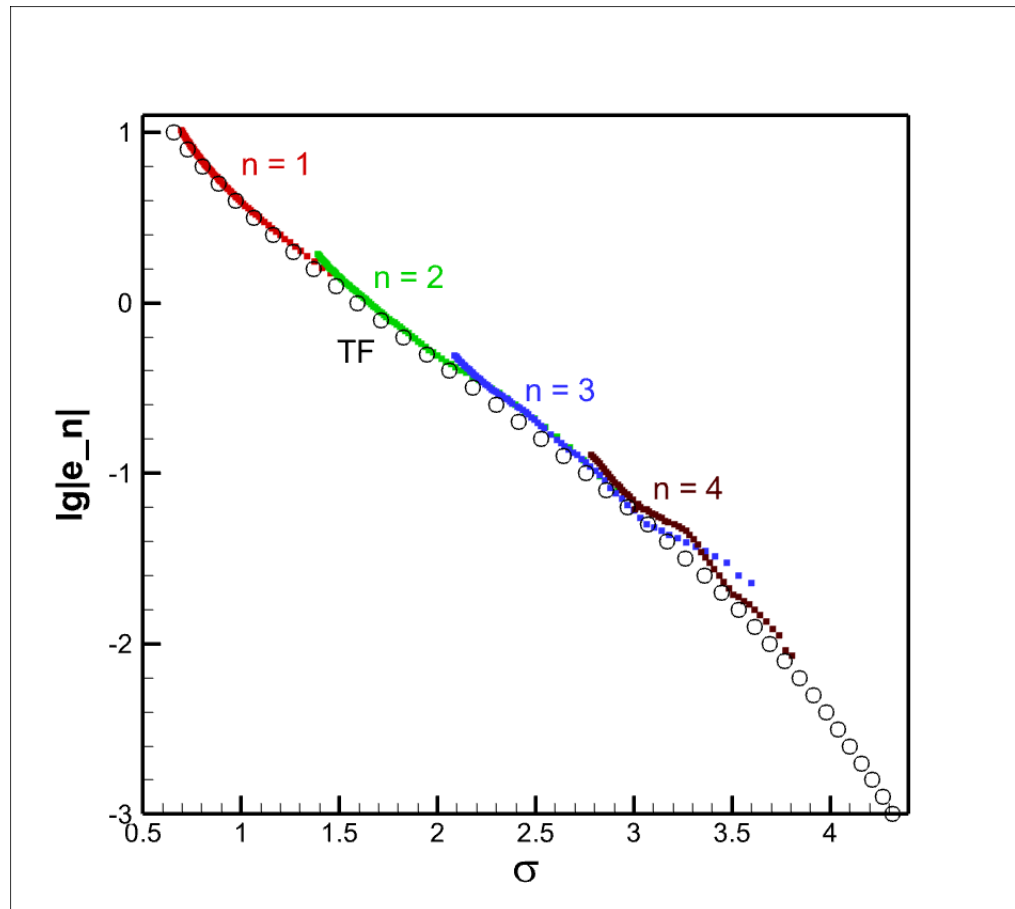


## 2.5 Functions $e(\sigma)$ , TF and reconstructed from all the experimental s-levels $E_{n0}$ for atoms $Z = 10 - 92$





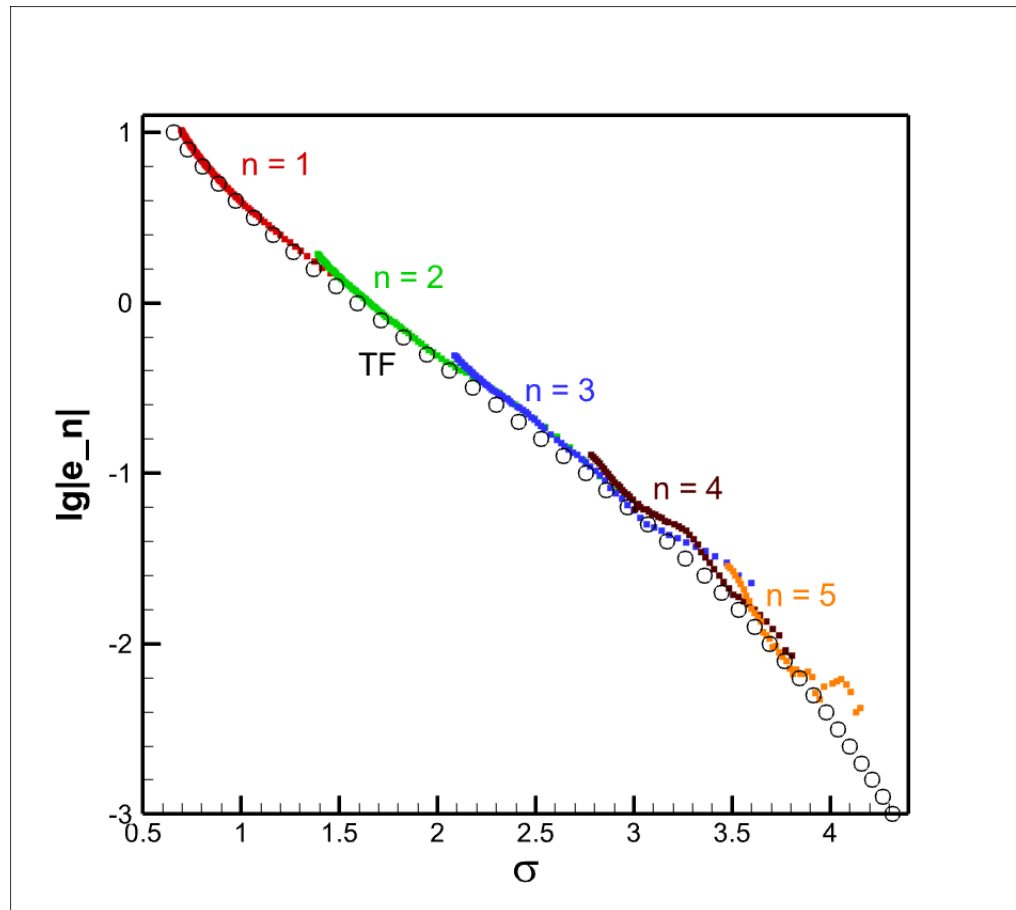
## 2.6 Functions $e(\sigma)$ , TF and reconstructed from all the experimental $ns$ -levels $E_{n0}$ for atoms $Z = 10 - 92$





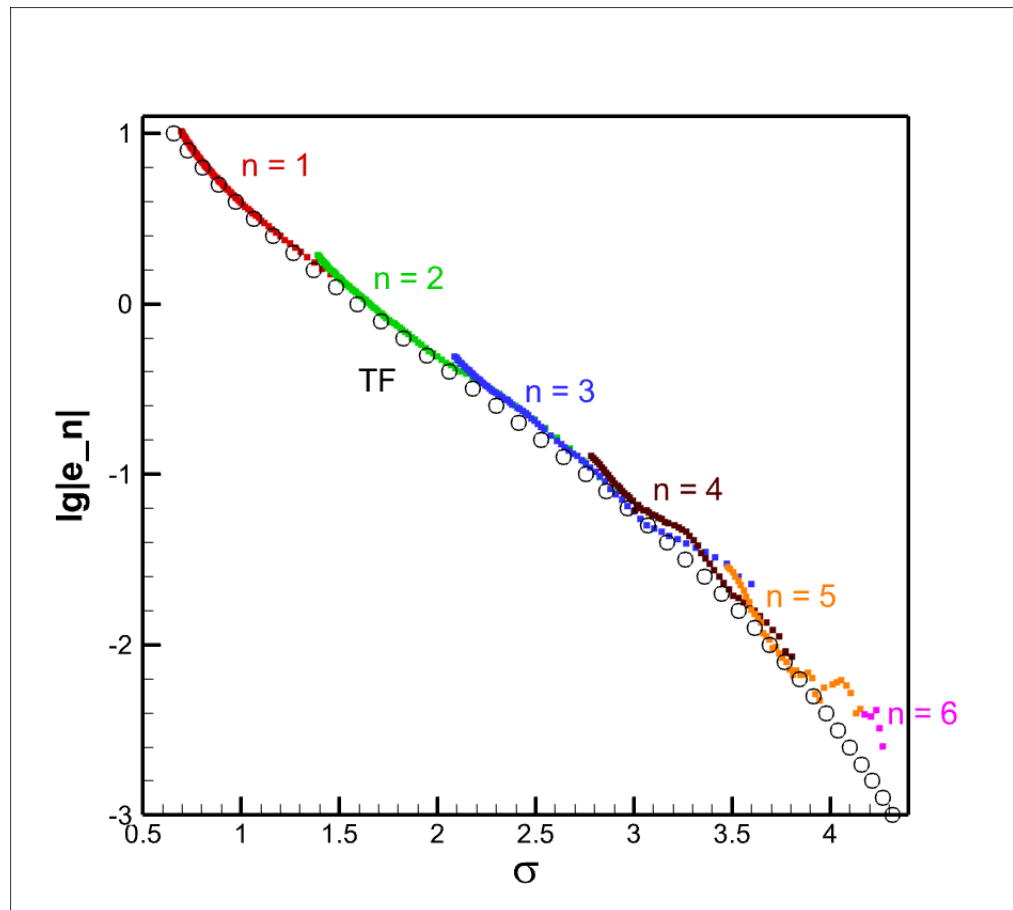


## 2.6 Functions $e(\sigma)$ , TF and reconstructed from all the experimental s-levels $E_{n0}$ for atoms $Z = 10 - 92$



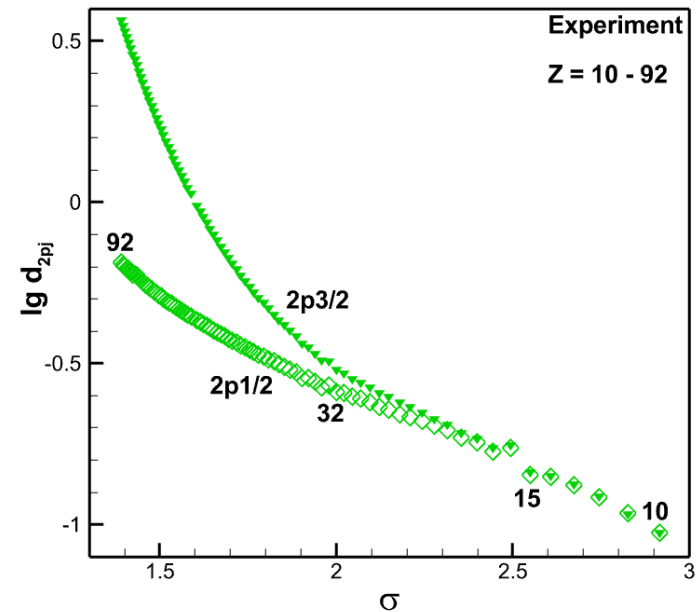
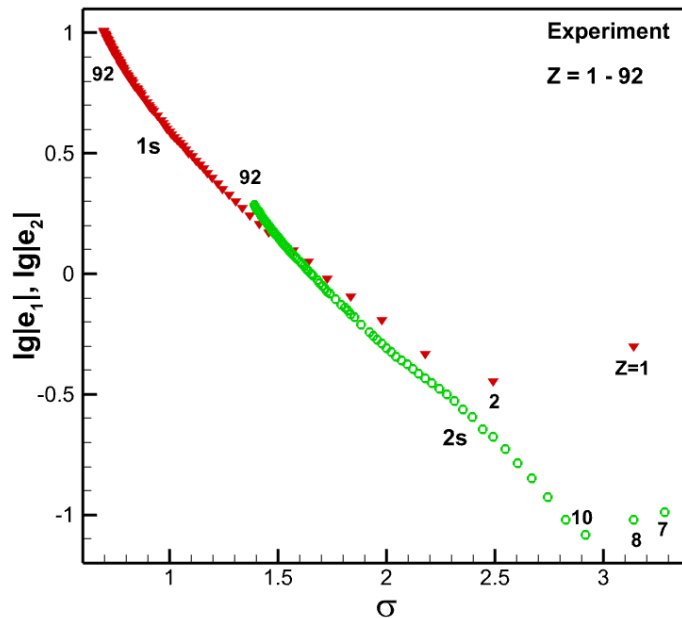


## 2.7 Functions $e(\sigma)$ : TF and reconstructed from all the experimental s-levels $E_{n0}$ for atoms $Z = 10 - 92$



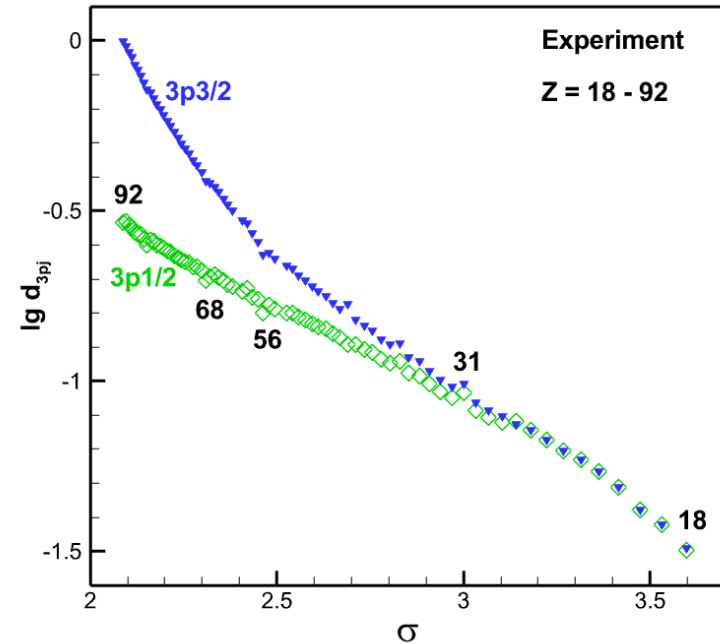
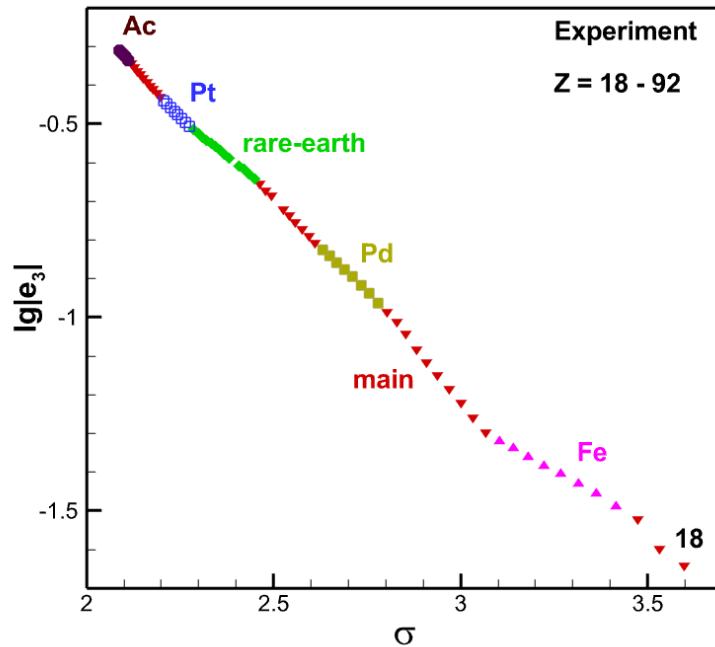


### 3.1 *K* and *L* shells. Electron binding energies (**EBE**) in all natural atoms $Z = 1 - 92$ from experimental data.



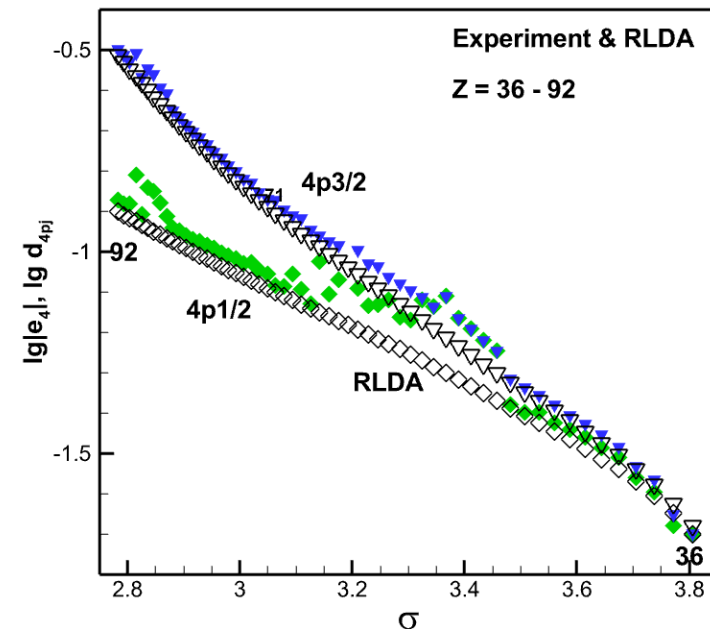
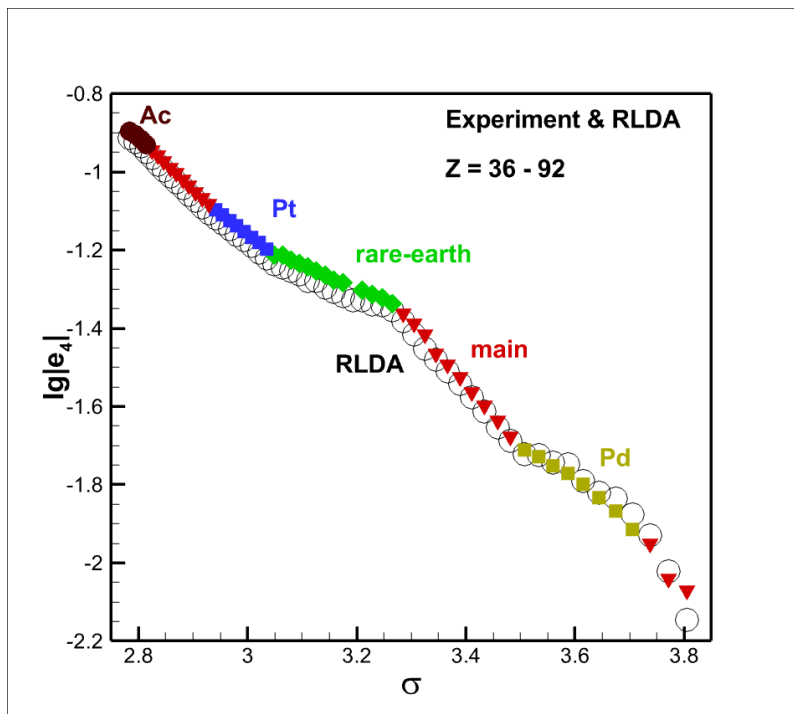


## 3.2 $M$ shell. Experimental **EBE** in the atomic groups (different color symbols)



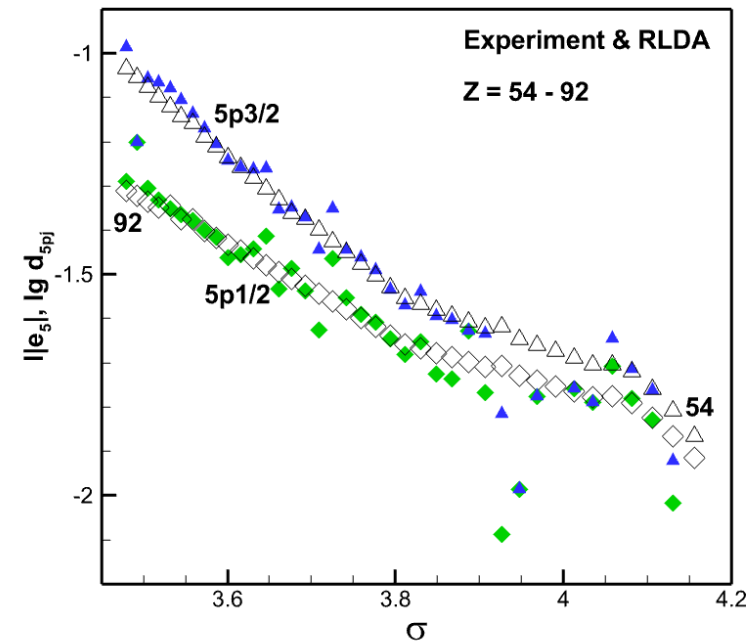
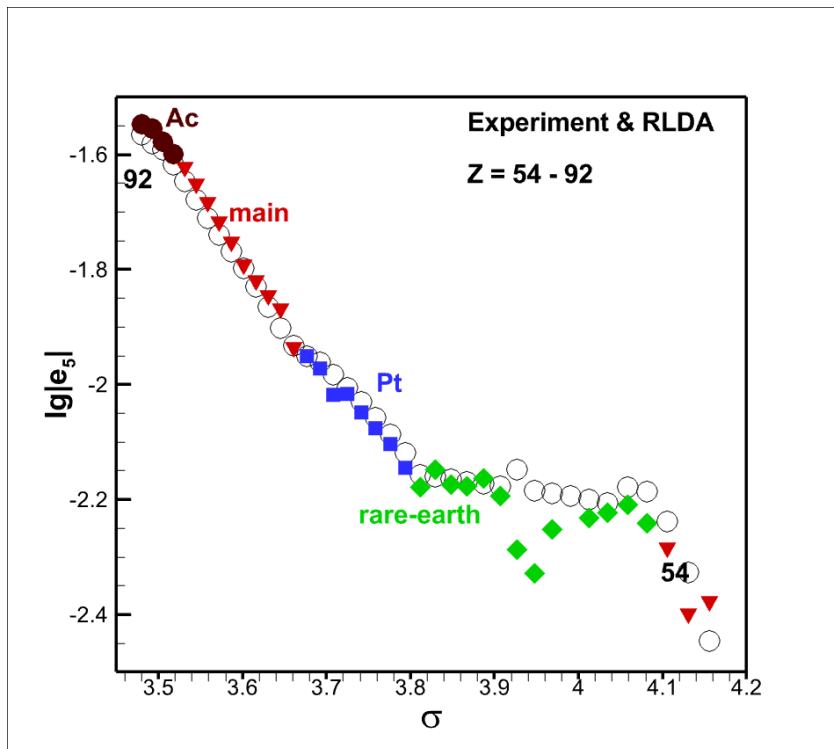


## 4.1 $N$ shell. Experimental (color symbols) and RLDA (black open symbols) **EBE**



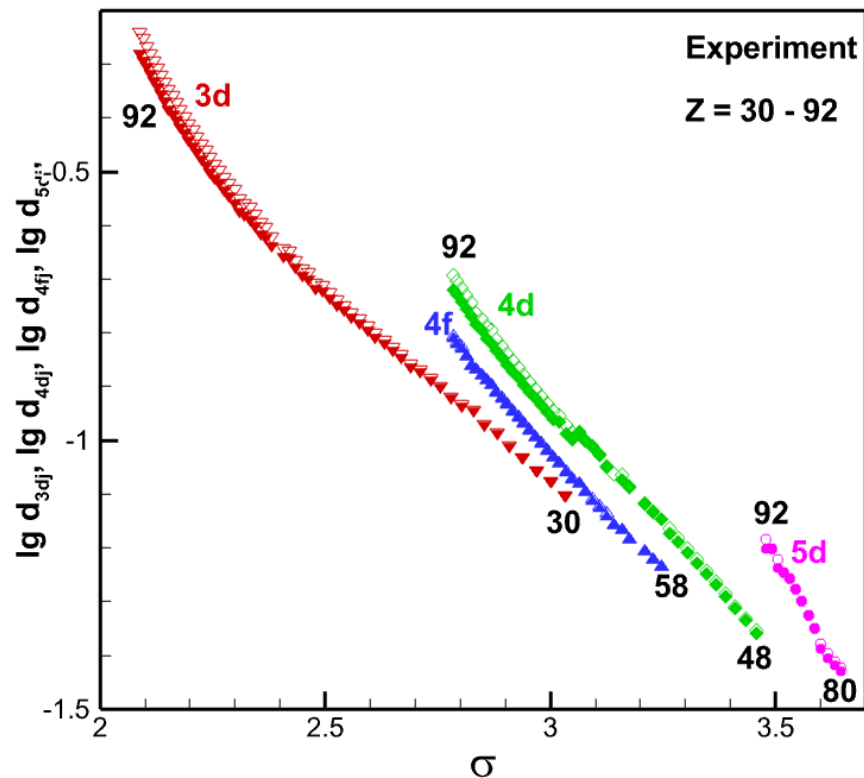


## 4.2 $O$ shell. Experimental (color symbols) and RLDA (black open symbols) **EBE**





## 4.3 Function $d(\sigma)$ for experimental **EBE** in subshells: 3dj, 4dj, 5dj, 4fj





## 5.1 Analytic approximation of experimental curves

- $\lg|e_n(\sigma)| = \sum_{k=0}^3 a_k^{(n)} \sigma^k$
- $\lg d_{nlj}(\sigma) = \sum_{k=0}^3 b_k^{(nlj)} \sigma^k$
- $E_{n0}(Z) = Z^{4/3} e_n(\sigma_n), \quad \sigma_n = \pi n Z^{-1/3}, \quad \text{if } l = 0;$
- $E_{nlj}(Z) = Z^{4/3} e_n(\sigma_n) + Z^{2/3} d_{nlj}(\sigma_n) \lambda^2, \quad \lambda = l + 1/2$





## 5.2 Analytic **EBE** estimates in comparison with data from other sources

**Table 2.** Orbital binding energies  $|E_{nlj}|$  (eV) estimated by equation (5) in comparison with experimental data from [3–5].

$Z$	$n$	$l j$	equation (5)	[3]	[4]	[5]
2	1	$s$	24.52	24.6		24.59
5	1	$s$	186.8	188.0	186.4–187.3	192.2
9	1	$s$	703.2	696.7	684.0–694.0	692.4
9	2	$s$	33.24		23.70–33.64	37.21
15	2	$s$	186.3	189.0	187.7–188.0	191.4
		$p 1/2$	129.7	136.0	130.3	135.1 <sup>a</sup>
		$p 3/2$	128.9	135.0	129.4–130.9	
16	2	$s$	228.3	231.0	229.2	232.1
		$p 1/2$	166.0	164.0	162.0–166.1	168.1 <sup>a</sup>
		$p 3/2$	164.3	162.0	162.9–164.8	
31	3	$s$	160.1	159.5	161.0	161.0
		$p 1/2$	107.4	103.5	106.1–108.7	107.1 <sup>a</sup>
		$p 3/2$	103.9	100.0	104.3–105.8	
48	4	$s$	109.4	109.8	109.8	112.4
83	4	$s$	939.5	939.0	939.0	940.8
76	5	$s$	87.84	84.0	94.6	87.1
85	5	$s$	193.2	195.0		194.7

<sup>a</sup> Excluding spin-orbit splitting.



## Examples of the method application

- Analytic **description** of experimental ***K*, *L*** X-ray **terms** in multi-electron atoms ( **$Z > 10$** ) and **control their reliability**
- **Analysis and correction** of experimental electron binding energies in **lanthanides**
- Discovering **patterns** in the measured **first ionization potentials** of **lanthanides and actinides**



## 6. Conclusions

1. The most **experimental EBE** in the reduced coordinates  $e(\sigma)$ ,  $d(\sigma)$  form **smooth dependences**, that is an **atomic number similarity law**.
2. The **deviation from the law** indicates a measurement error.
3. The found **atomic number similarity law** provide a way to **recover missing or erroneous data** with an accuracy  $\sim 1\%$ .
4. The available theoretical **RLDA model** does not satisfactorily describe the **EBE**.



# Thank you for attention!

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